

# Managing Climate Risks

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# Key Points

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- Why Risk Management?
- Total Uncertainty = Model + Parameter
- Climate Damage: Inner and Outer Measure

# Rational Decision Theory

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- A rational agent maximizes expected utility
- (subjective) probability and utility unique *to individual*
- Climate change is a group decision problem
- Professional risk takers don't manage risk by bending the utility function of a 'representative consumer'
- Probabilistic Design: optimize performance under risk constraint

# Risk Management Approach

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## ★ Risk-averse representative consumer

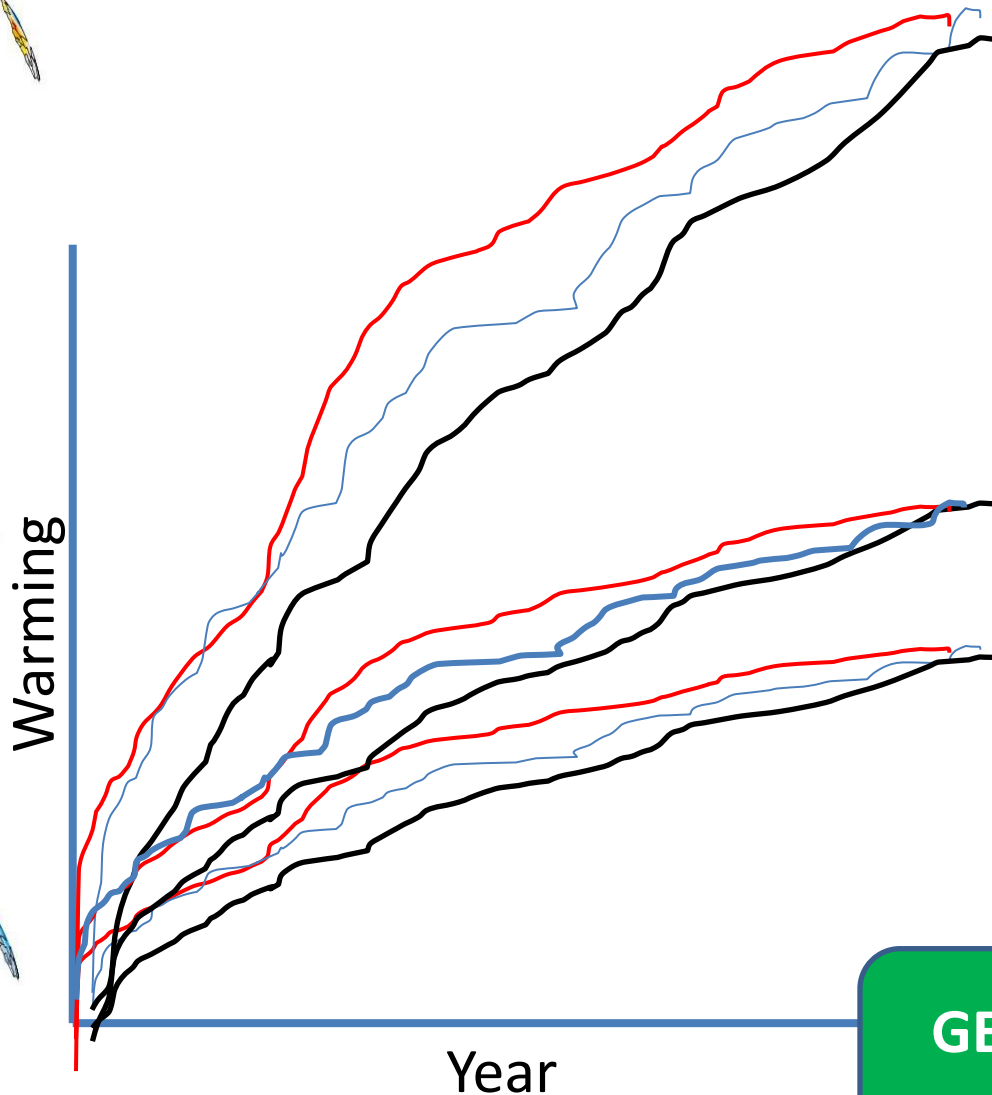
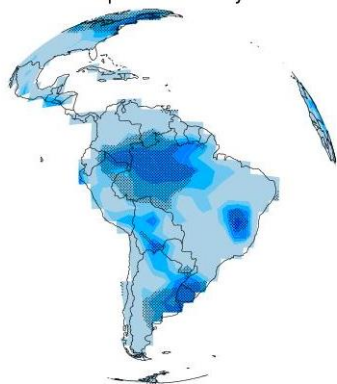
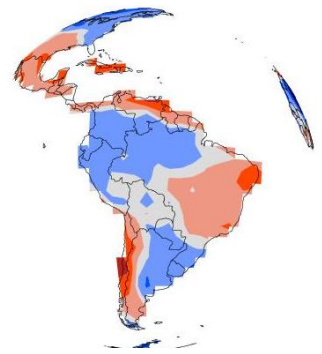
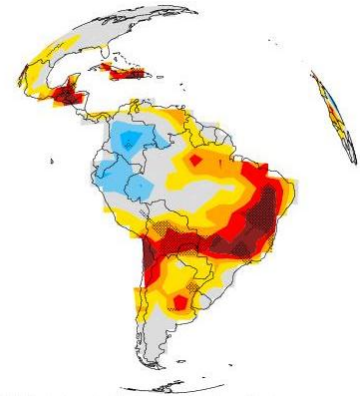
And / Or

- Discounting
- Utility function
- Utility of civilization

## ★ Risk-constrained optimization

- Capture total uncertainty
- Choose probability constraints for set of DAI's
- Find efficient ways to satisfy constraints

# Pricing Carbon at the Margin



Assume values of  
climate variables

Compute path

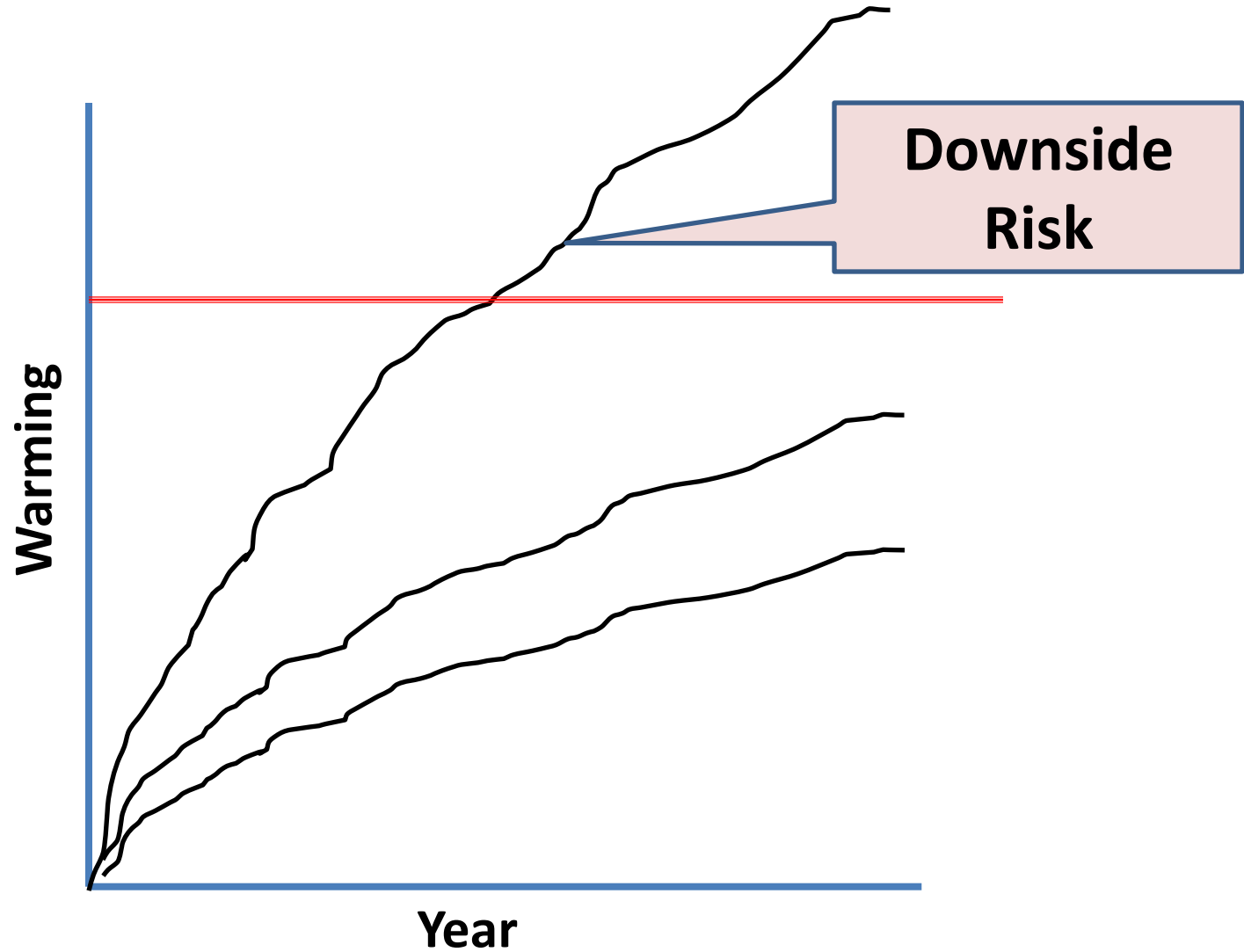
Compute NPV of  
damages from  
 $\Delta 1 \text{ t C}$

Different damage  
model

Different SOW

GET distribution over  
marginal cost of carbon

# Buying Down Risk



# Model Uncertainty

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- Stress test
- Canonical variations

# Stress Test DICE Growth Model

$\Lambda$  = abatement,  $A$  = total factor productivity,  $K$  = capital stock,  
 $N$  = labor,  $\delta$  = depreciation

$$\text{Output}(t) = \frac{[1-\Lambda(t)] A(t) K(t)^\gamma N(t)^{1-\gamma}}{(1 + .0028\text{Temp}(t)^2)}$$

$$K(t+1) = (1-\delta) K(t) + \text{Output}(t) - \text{Consump}(t)$$

**Bernoulli Equation**  $\text{Consump}(t) = \eta(t)\text{Output}(t)$  :

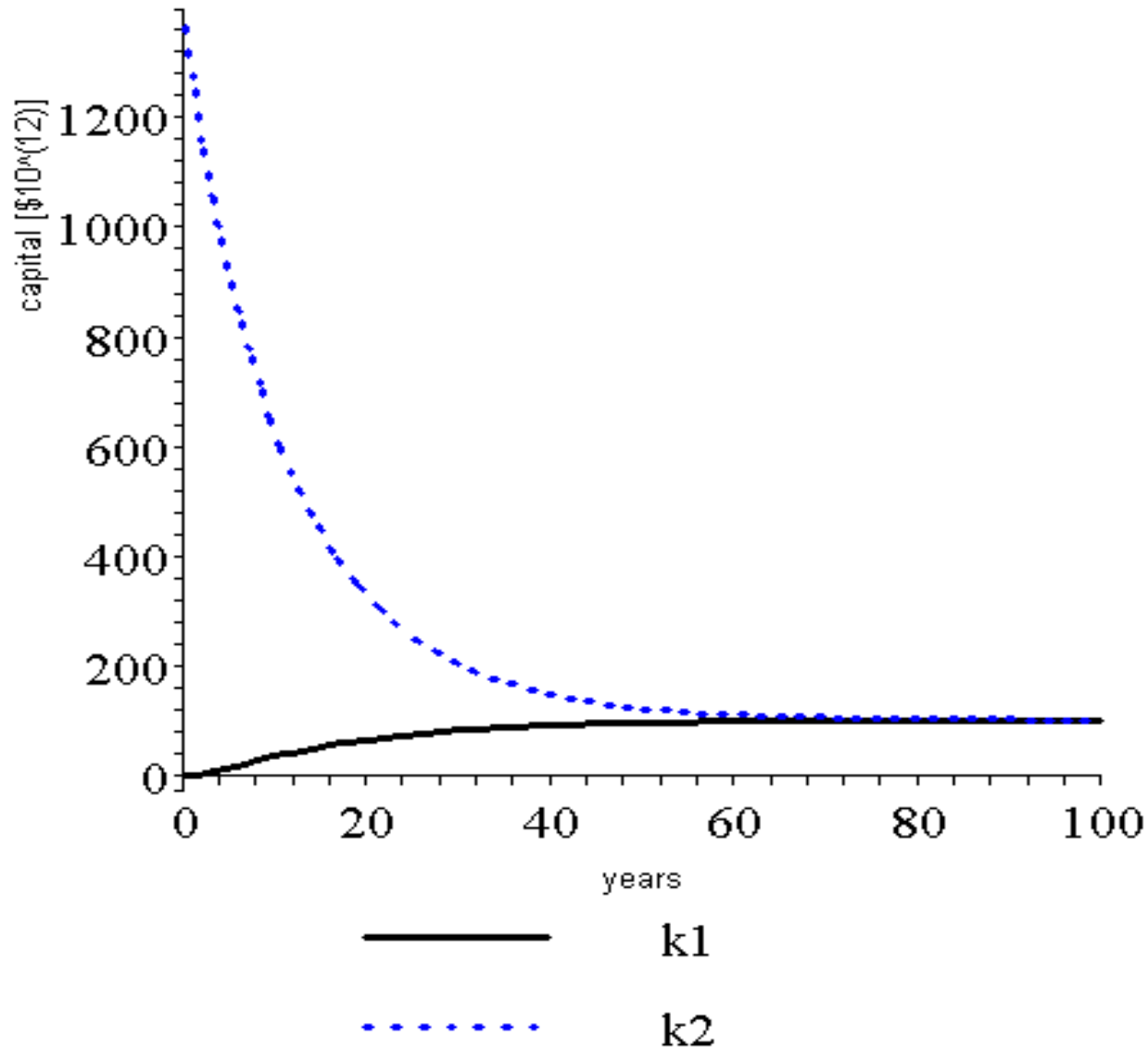
$$dK/dt = -\delta K(t) + B(t)K(t)^\gamma;$$

Put  $\text{Temp}(t) \equiv 0$ ;  $A(t) \equiv A$ ;  $N(t) \equiv N$ ;  $\Lambda(t) \equiv 0$ ;  $\eta(t) \equiv \eta$

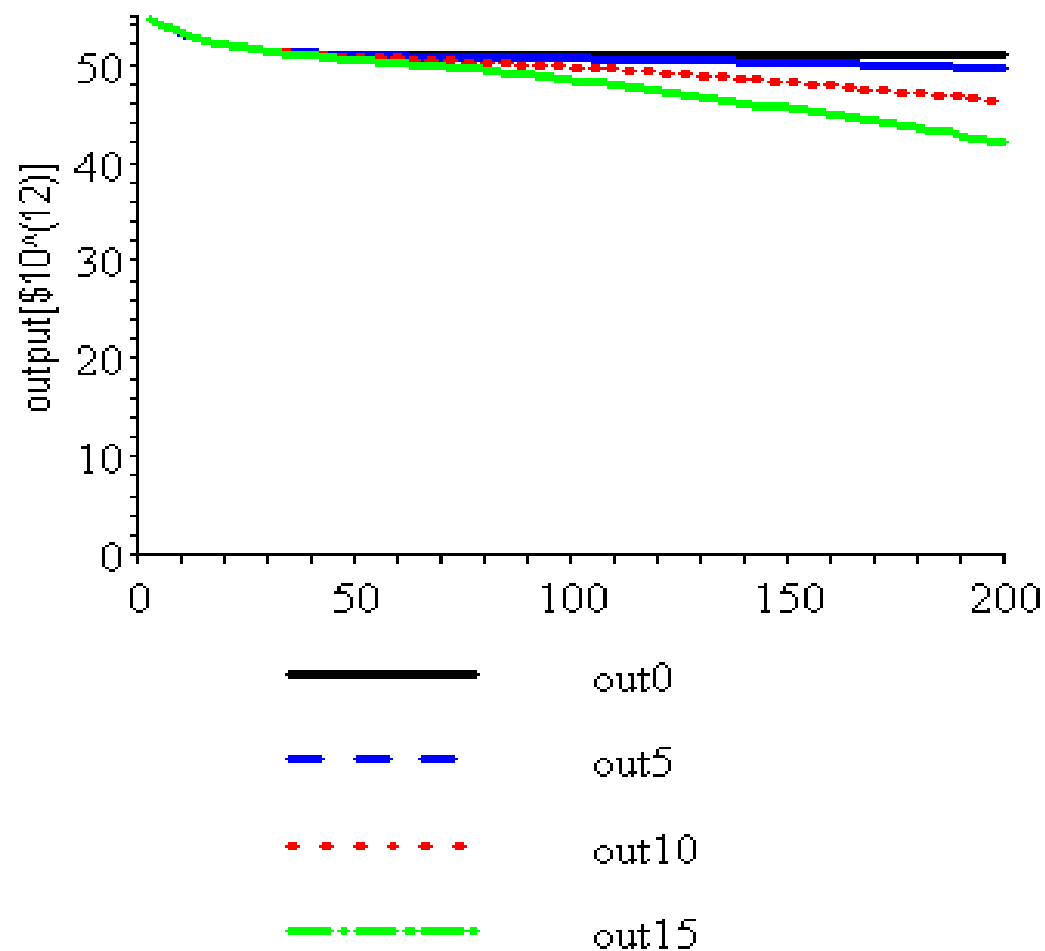
$$K(t) = [(1-\gamma) B \int_{x=0..t} e^{-(1-\gamma)\delta x} dx + e^{-(1-\gamma)\delta t} K(0)^{(1-\gamma)}]^{1/(1-\gamma)}$$



**Two capital trajectories with DICE values,  
no temperature rise, no abatement  
 $K1(0) = 1\$$  and  $K2(0) = 1370$  trillion  $\$$**



**Output[Trill \$], outx(t) is output at time t  
with linear temperature increase of x [C] in 200 years  
with starting capital C = 137 [Trill \$]**



# Canonical Variations

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- Do other simple model forms  
have structurally different behavior?

# Lotka Volterra instead of Bernoulli Model

$$\text{GHG}(t+1) = (1 - 0.0083)\text{GHG}(t) + 0.024 \times \text{GWP}(t)$$

**Emissions proportional to  
Gross World Output**

(Kelly & Kohlstadt 2001)

$$\text{GWP}(t+1) = [1 + 0.03 - D(T(\text{GHG}(t)))] \times \text{GWP}(t)$$

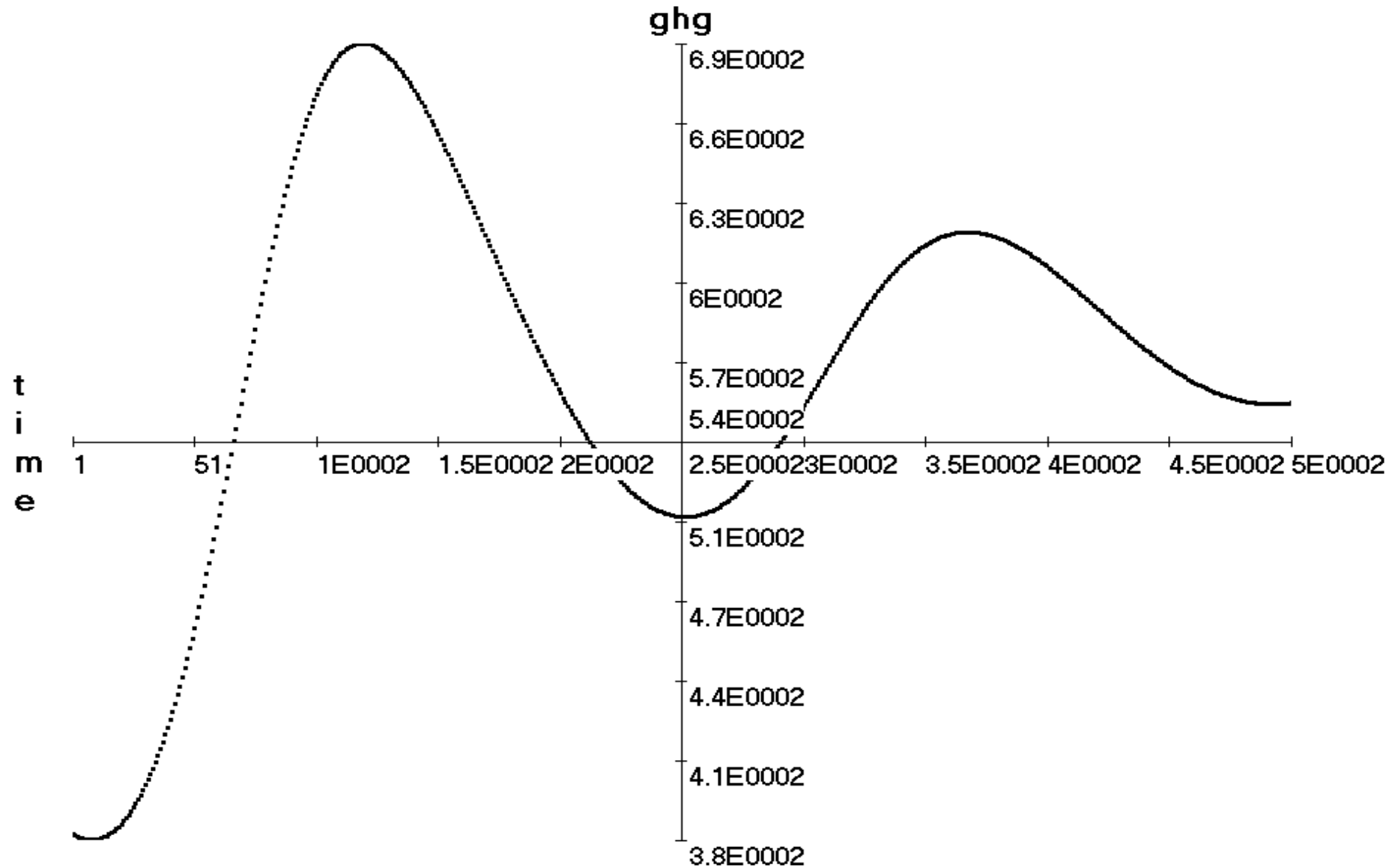
**Gross World Output  
Growth Rate**

(World Bank, last 48 yrs)

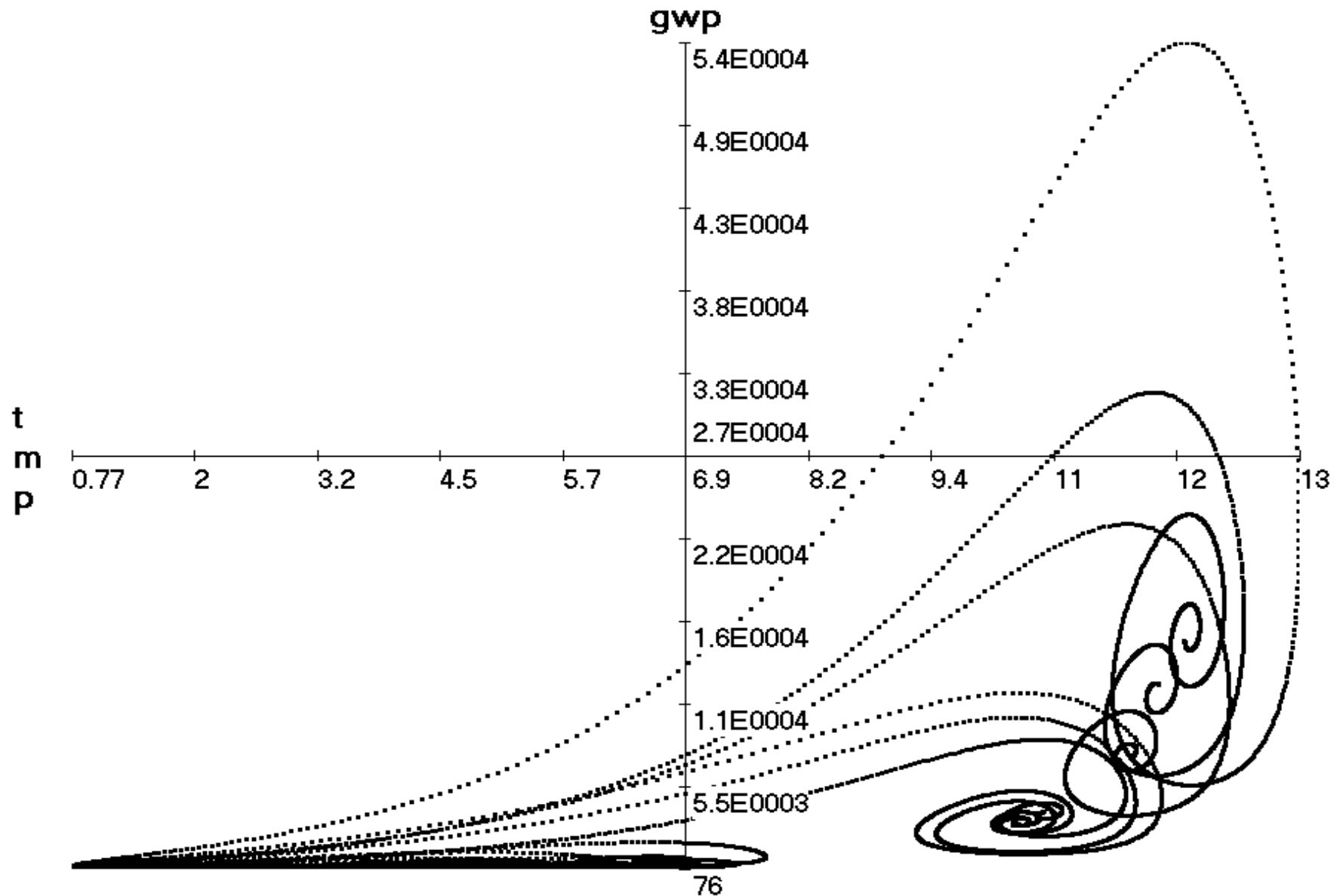
$$D(\text{GHG})(t) = (T/18)^2$$

**Weitzman's Death  
Temperature**

# Different Behavior

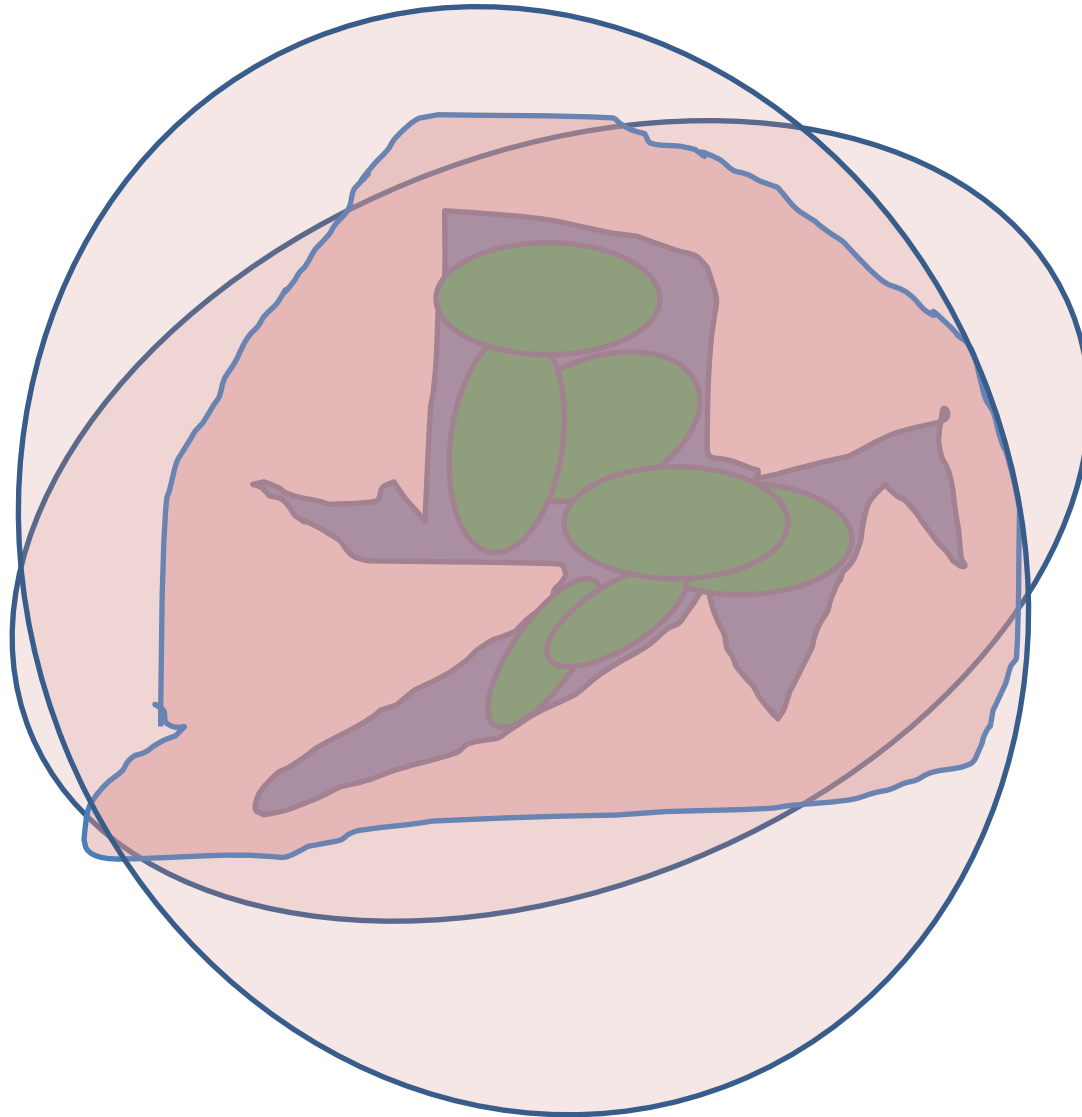


# Phase Portraits, w / wo Dependence



# Damage: Inner & Outer Measure

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# Deal with Model Uncertainty?

- Fit your models to ~~data~~?
- Fit your models to probabilistic data from Structured Expert Judgment
- Bayes Model Averaging
- ....



# Yale G-Econ Database: Gross Cell Product

GCPpp Time average growth rate:  
$$[\ln(\text{GCPpp}) - \min[\ln \text{GCPpp}]] / 400$$

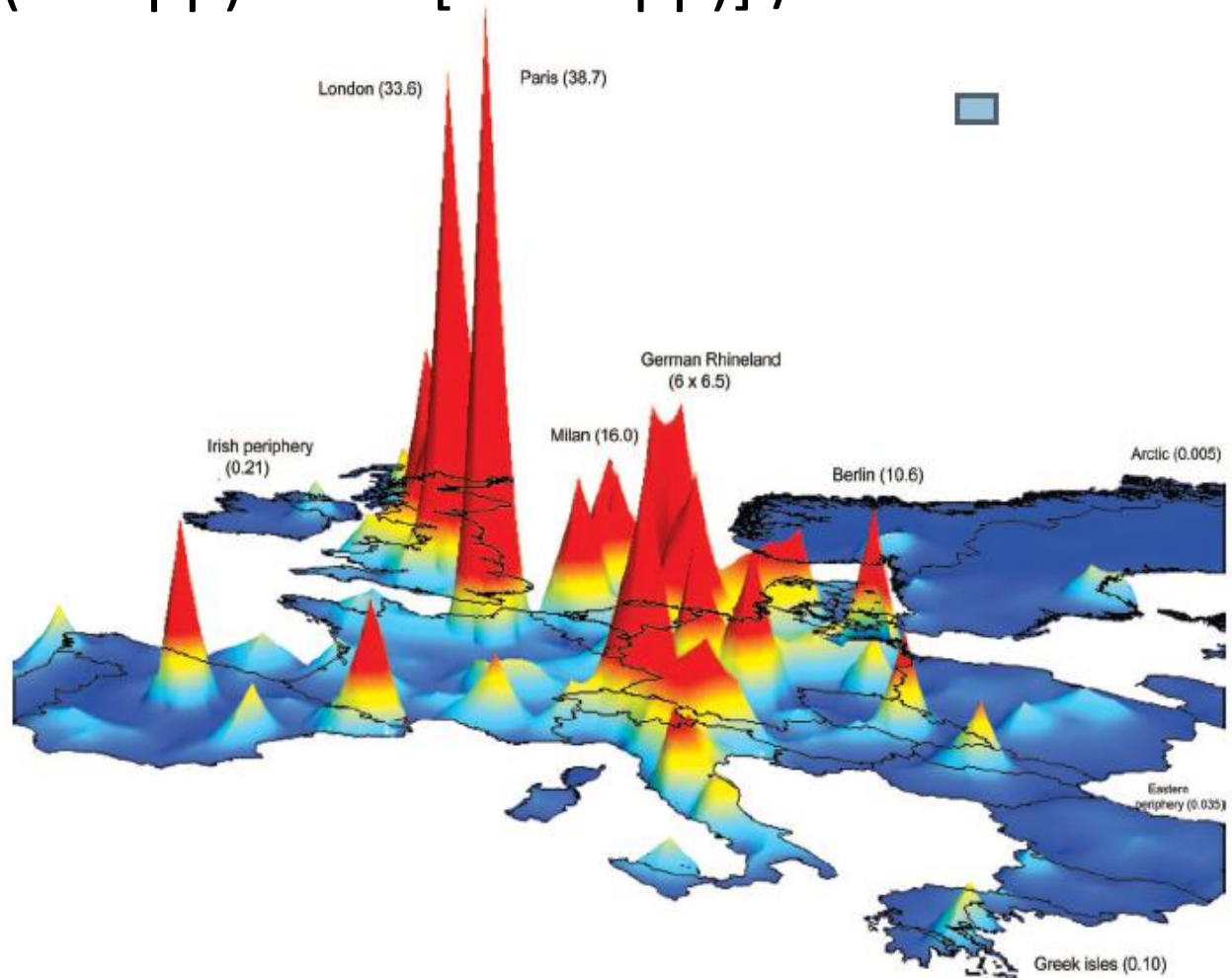
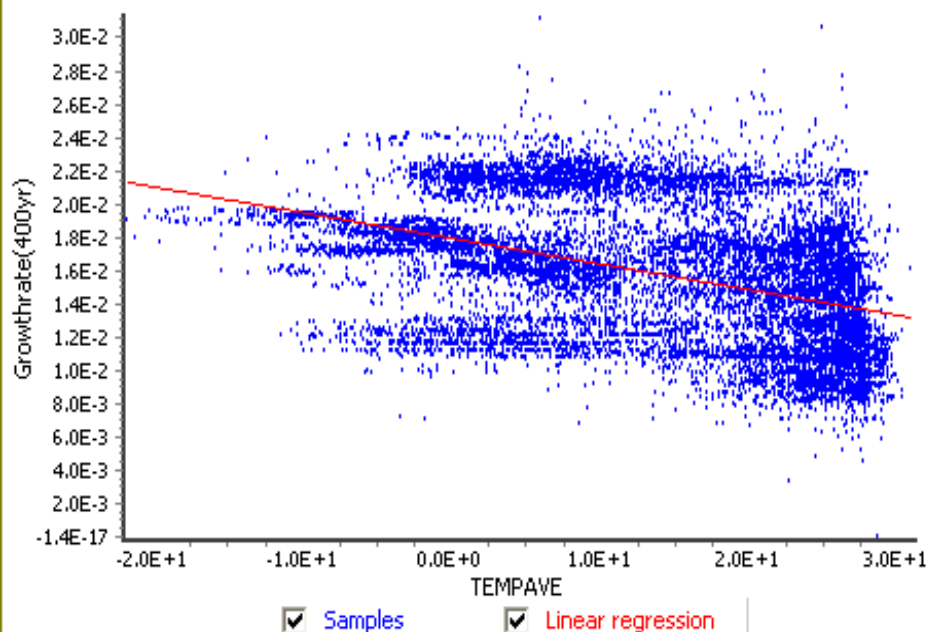
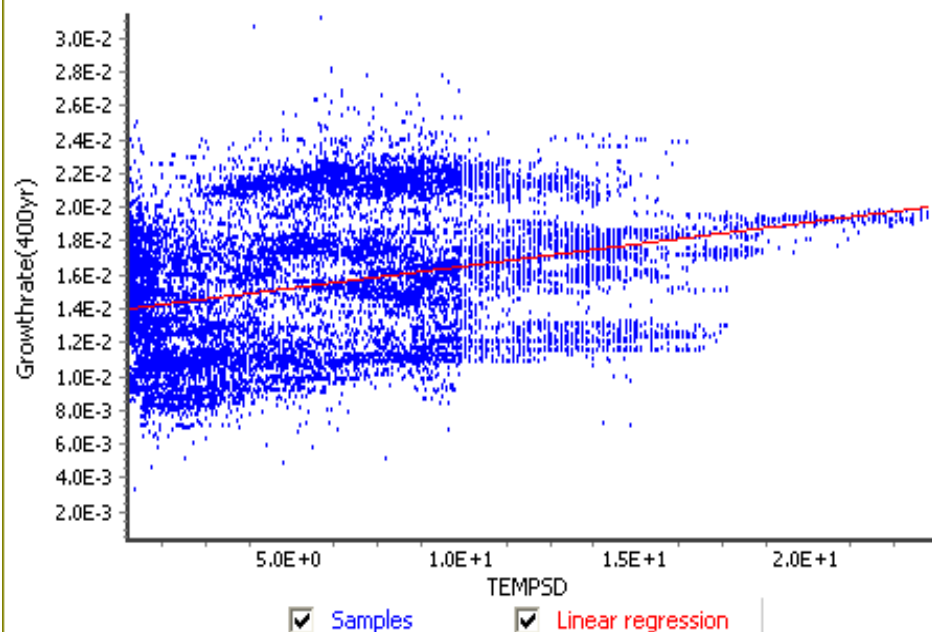


Fig. 1. Economic map of Europe. This figure shows an economic topographical map of Europe with heights proportional to gross domestic product per area. Note how economic activity clusters in the core, whereas the periphery has much lower economic elevations. The observations measure economic activity in millions of 1995 U.S. dollars per km² at a 1° latitude by 1° longitude scale.

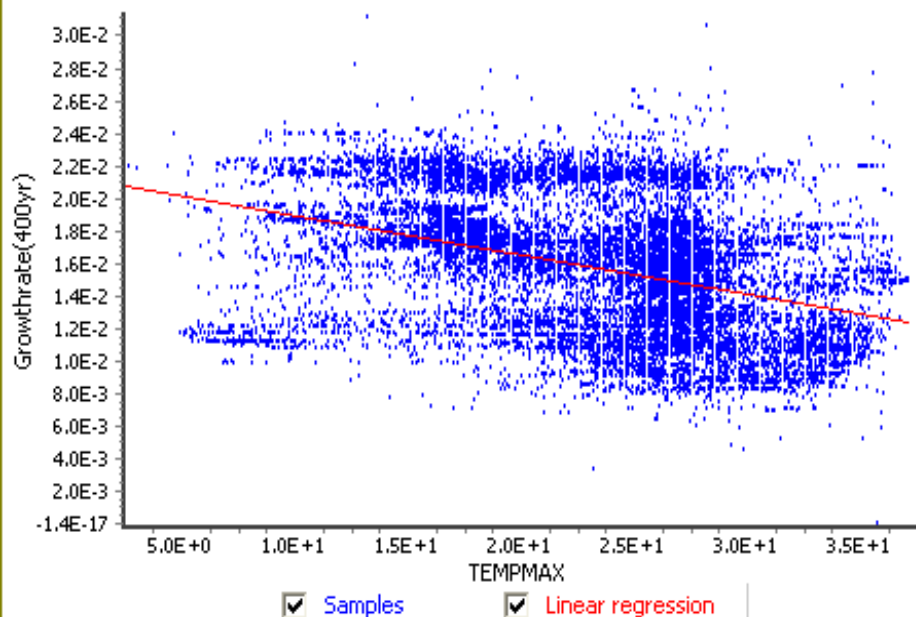
Regression of Growthrate(400yr) on TEMPAVE



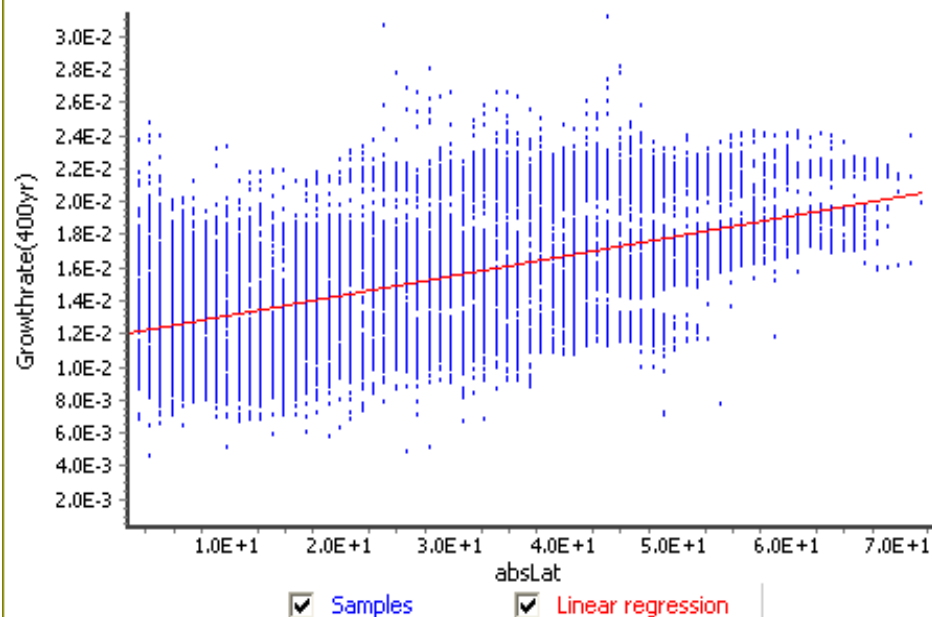
Regression of Growthrate(400yr) on TEMPSD



Regression of Growthrate(400yr) on TEMPMAX

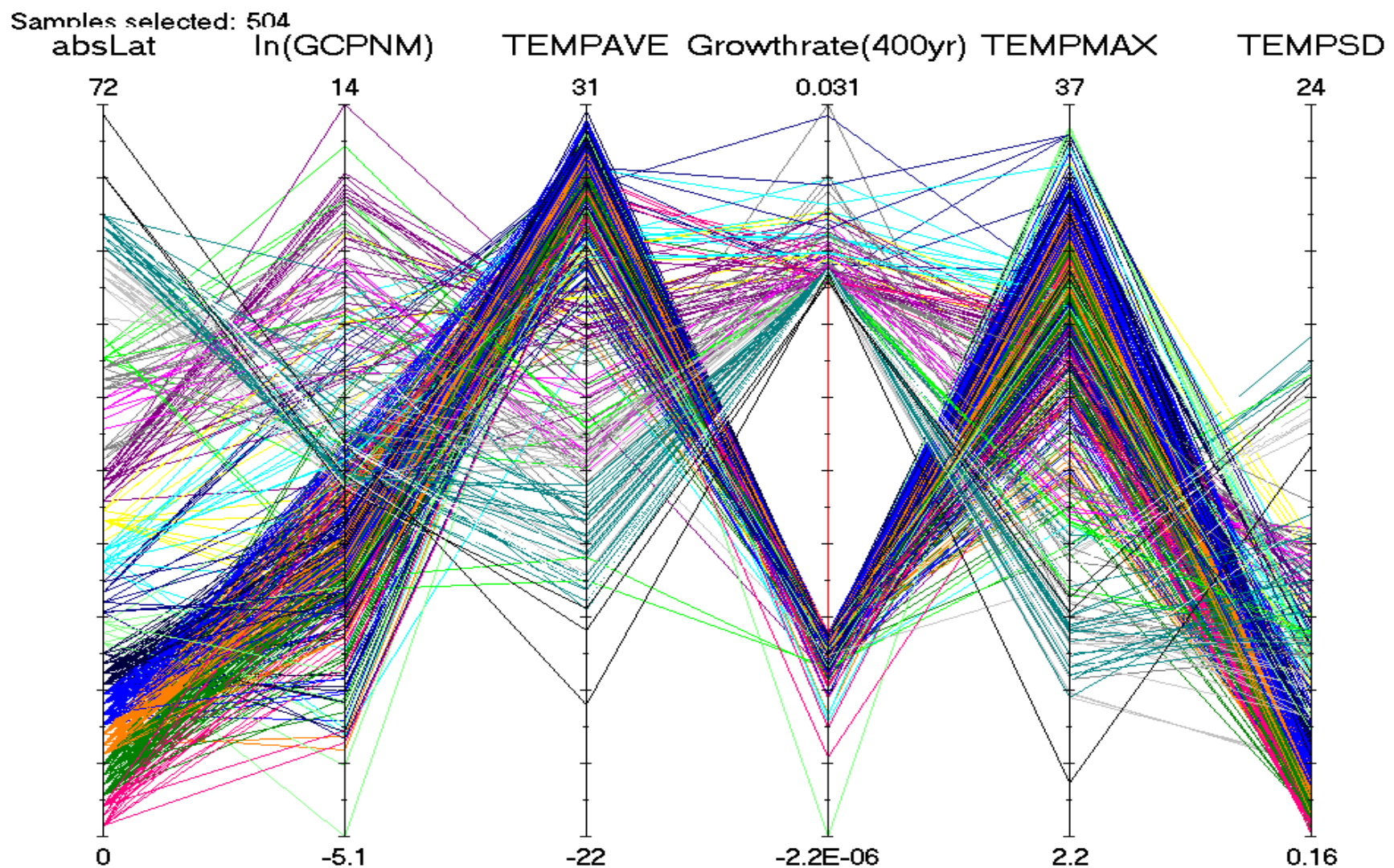


Regression of Growthrate(400yr) on absLat



# Joint Distribution as Cobweb Plot

## Conditional on top and bottom 1% growth rates



## Factor multiplying GCPpp when changing only TEMPAVE +3C

	<b>Indep Vbl</b>	<b>Covariate</b>	<b>Partial reg coeff</b>	<b>Factor</b>
Model 1	ln(GCPpp)	TEMPAVE	-0.06167	0.831095973
Model 2	ln(GCPpp)	absLat TEMPAVE TEMPMAX	0.083428 0.109418 -0.09706	1.388541617
Model 3	ln(GCPpp)	absLat TEMPAVE TEMPMAX TEMPSD	0.088856 -0.038029 0.047788 -0.222984	0.892180333
Model 4	ln(GCPpp)	TEMPAVE TEMPMAX TEMPSD	-0.121162 0.041572 -0.103743	0.695248461



# Conclusions

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- Need to tackle model uncertainty
- Need to converge 'inner' and 'outer' damage models

# What Are Predicted Impacts of Warming?

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- 5°C

- collapse of Greenland ice sheet
- large-scale eradication of coral reefs
- disintegration of West Antarctic ice sheet
- shut-down of thermohaline circulation
- millions of additional people at risk of hunger, water shortage, disease, or flooding

*(Parry, Arnell, McMichael et al. 2001; O'Neill and Oppenheimer 2002; Hansen 2005)*

- 11-12°C

- regions inducing hyperthermia in humans and other mammals  
“would spread to encompass the majority of the human population as currently distributed”

*(Sherwood and Huber 2010)*

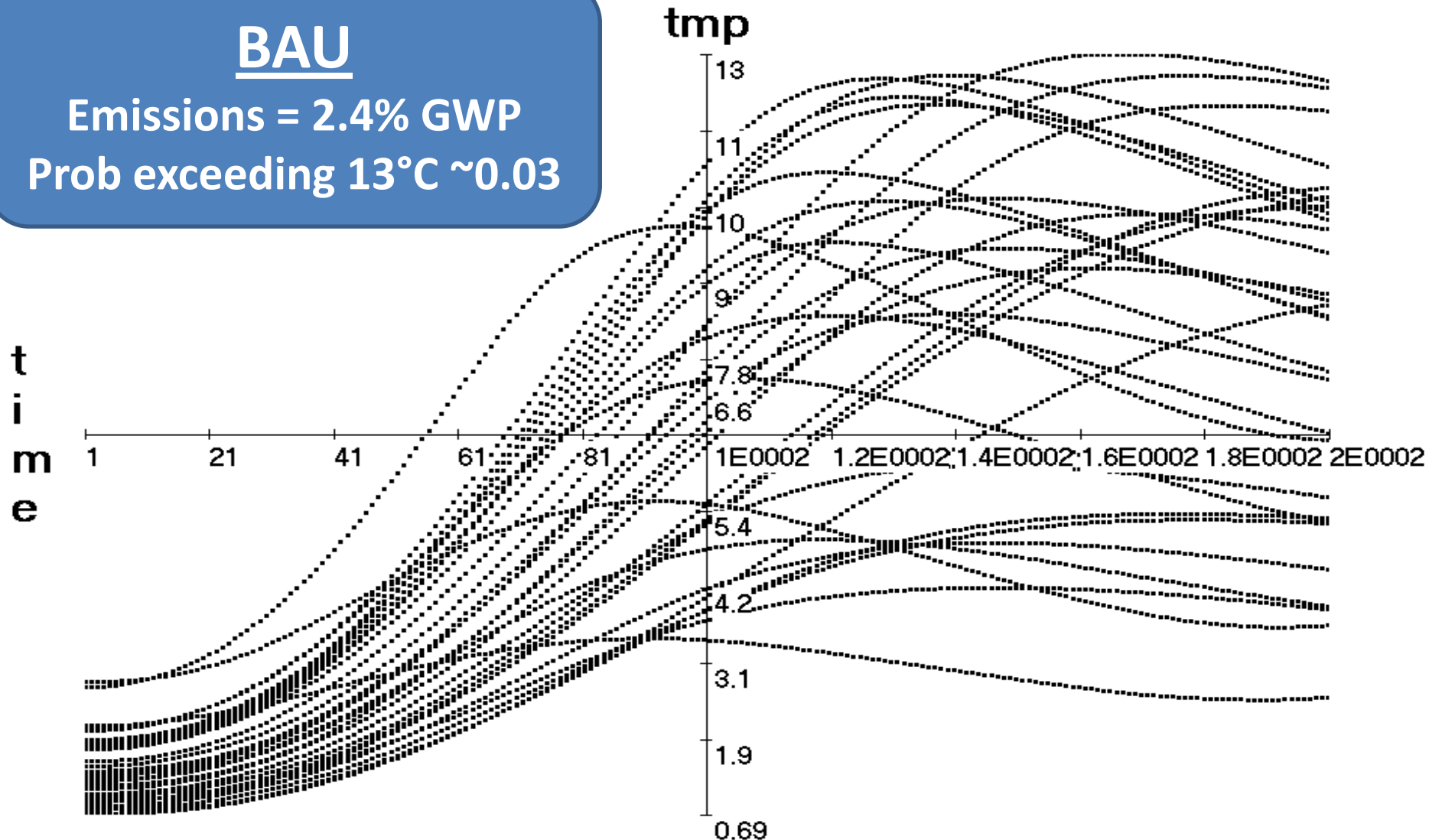
# Value@Risk (*Basel II Protocol*)

Banks reserve capital to cover “1-in-200 yr” loss event

BAU

Emissions = 2.4% GWP

Prob exceeding 13°C ~0.03



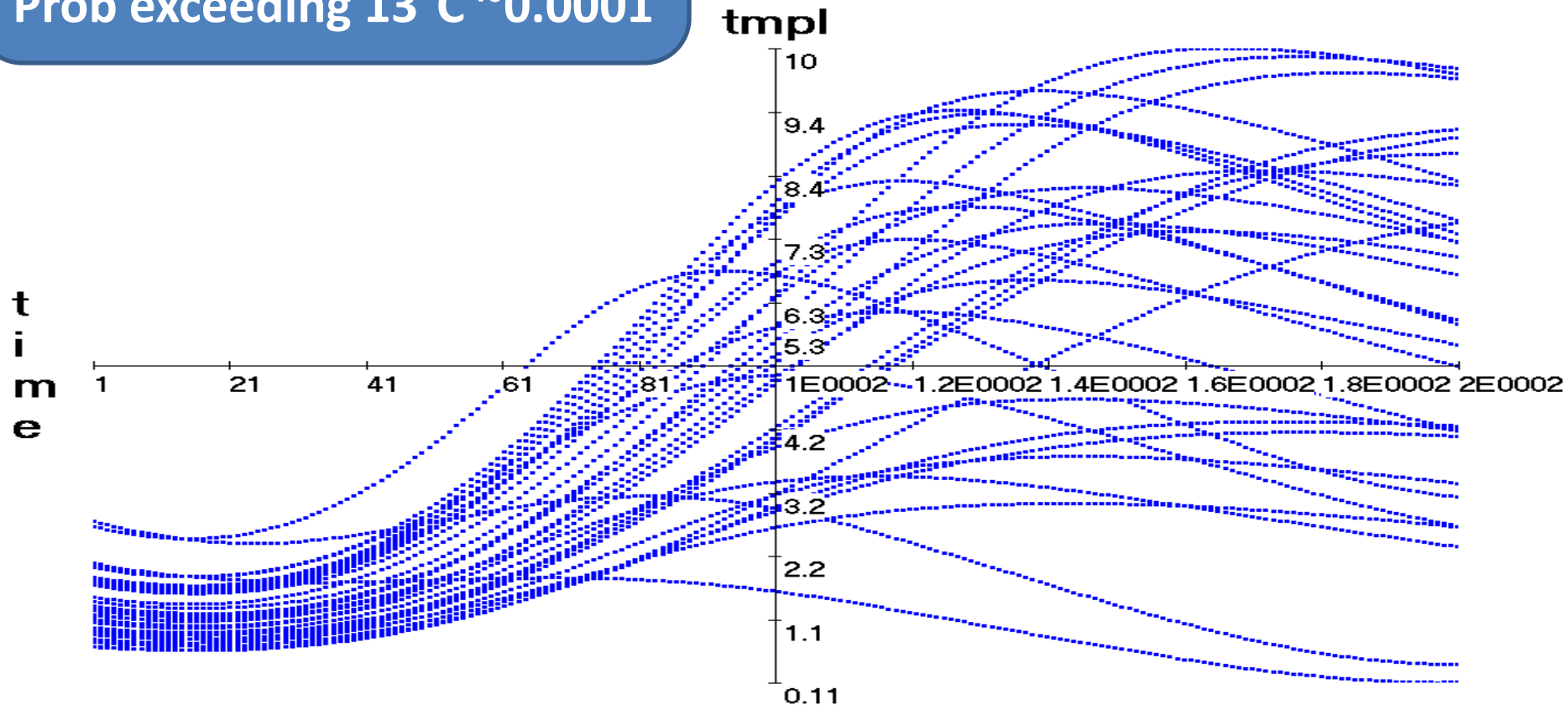
# Value@Risk (*Basel II Protocol*)

Banks reserve capital to cover “1-in-200 yr” loss event

## Stringent

Emissions = 1.5% GWP

Prob exceeding 13°C ~0.0001





# Risk Constraints

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- $\text{PROB}\{\Delta T > 13^{\circ}\text{C for } 500 \text{ yr}\} < 0.0001$
- $\text{PROB}\{\text{Greenland ice sheet melts in } 300 \text{ yr}\} < 0.001$
- $\text{PROB}\{\text{Oceans become net C emitter in } 100 \text{ yr}\} < 0.01$
- ***What is the price?***